

RECENT DEVELOPMENTS IN LIPSCHITZ GLOBAL OPTIMIZATION¹

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In this lecture, the global optimization problem of a multidimensional function satisfying the Lipschitz condition over a hyperinterval with an unknown Lipschitz constant is considered. It is supposed that the objective function can be “black box”, multiextremal, and non-differentiable. It is also assumed that evaluation of the objective function at a point is a time-consuming operation. Many algorithms for solving this problem have been discussed in literature (see [1–8] and references given therein). They can be distinguished, for example, by the way of obtaining information about the Lipschitz constant and by the strategy of exploration of the search domain. Different exploration techniques based on various adaptive partition strategies are analyzed.

The main attention is dedicated to two types of algorithms: (i) methods using space-filling curves to reduce the dimensionality of the global optimization problem; (ii) diagonal global optimization algorithms. Both classes of methods have a number of attractive theoretical properties and have proved to be efficient in solving applied problems. Several families of deterministic derivative-free numerical algorithms are discussed. A number of unconventional ideas, such as adaptive strategies for estimating Lipschitz constant, balancing global and local information to accelerate the search, etc. are presented. Results of extensive numerical experiments performed on the GKLS-generator (see [1]) demonstrate advantages of the proposed methods with respect to a number of traditional algorithms.

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¹This research was partially supported by the INdAM–GNCS 2014 Research Project of the Italian National Group for Scientific Computation of the National Institute for Advanced Mathematics “F. Severi”.